



TECHNISCHE UNIVERSITÄT
BERGAKADEMIE FREIBERG

Die Ressourcenuniversität. Seit 1765.

A Conceptual Study of Mining Subsidence Analysis



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Chair of Engineering Geology, Disposal Facilities and Geotechnical Securing Methods

Mining Subsidence Analysis:

**Scientific field in the cross section
between Geodesy and Geotechnics**

**The observation of deformations
in the ground massive under
mining exposure delivers
extensive information quantity**

Classical methods of mining subsidence analysis

Classical methods of mining subsidence analysis:

**Verified empirical and stochastic
hypothetical ground deformation models
of mining induced displacements**

**Calibration on geodetic deformation
measurements leads to a solid basis
for displacement prediction with
synthetic forward models**



Advanced methods of mining subsidence analysis

Advanced mining subsidence analysis:

Deformation prediction for the mining influenced region is a difficult soil and rock mechanics (geotechnic) problem

Advanced analysis methods of Geotechnics offer the opportunity to solve the time independent or time dependent initial and boundary value problem

Mining subsidence analysis and deformation prediction with advanced analysis methods of Geotechnics

Modell formulation for geotechnic mining subsidence analysis:

Geological, hydrogeological and geotechnical model

Profound characterization of the initial (geostatic) stress state and stress history

Sequence of primary and secondary deformation processes due to mining

Conceptual study of a classical problem in mining subsidence analysis with advanced analysis methods of Geotechnics (Qualitative analysis)

Geotechnic mine subsidence analysis:

Axialsymmetric model

Model radius: 50m

Radius of primary displacement: 10m

Amplitude of primary displacement: 1m

Model height: 30m und 50m

Geotechnic mine subsidence analysis:

**Material model: Drucker-Prager
without hardening or softening**

**Stiffness formulation: depending on the
initial stress state but constant at loading**

No volume change during shear failure

Drucker-Prager strength parameters:

$$\text{ALFA} = \text{ETA} = \frac{2 \sin(\varphi)}{\sqrt{3} (3 + \sin(\varphi))} , \quad \text{BETA} = \text{MU} = \sqrt{\frac{2}{3}} ,$$

$$\text{K} = \text{KL} = \frac{6 c \cos(\varphi)}{\sqrt{3} (3 + \sin(\varphi))} ,$$

$$\text{GAMM} = \frac{2 \sin(\psi)}{\sqrt{3} (3 + \sin(\psi))} , \quad \text{DELT} = \sqrt{\frac{2}{3}}$$

Drucker-Prager stress dependent (but constant) stiffness parameters:

$$YOUNG = E = E_{\text{ref}} \left(\frac{p'}{P'_{\text{ref}}} \right)^m$$

$$p' = \frac{1}{3} \text{tr}(\sigma')$$

Geotechnic mining subsidence analysis:

No layering (here)

No anisotropy (here)

No fluid influence (here)

No time dependent behaviour (creep)

Geotechnic mining subsidence analysis:

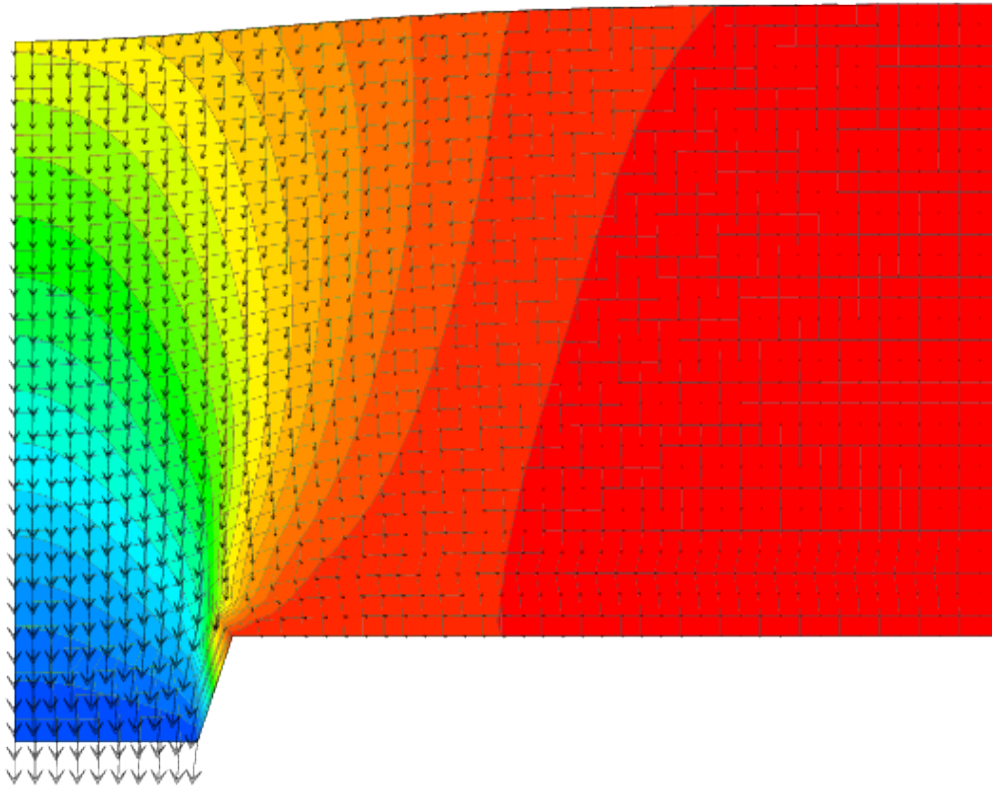
Model height: 30m

Stiffness: low

Material: cohesive (clay)

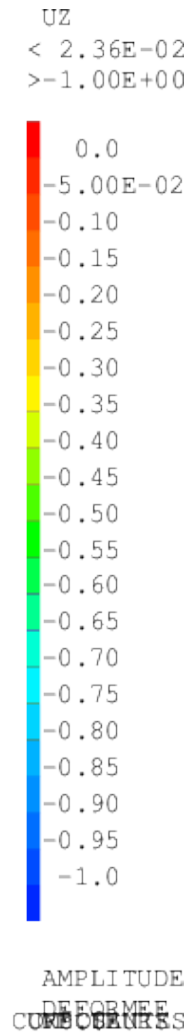
Mining subsidence – Vertical displacement:

$$u_1 = 0,338 \text{ [m]}$$



$$u_0 = 1,000 \text{ [m]}$$

u_z



Drucker-Prager:

$$\rho = 2000 \text{ [kg/m}^3\text{]}$$

$$\varphi = 10,00 \text{ [}^\circ\text{]}$$

$$c = 10,00 \text{ [kN/m}^2\text{]}$$

$$\psi = 0,00 \text{ [}^\circ\text{]}$$

$$E_{\text{ref}} = 10^6 \text{ [kN/m}^2\text{]}$$

$$p_{\text{ref}} = 10^5 \text{ [kN/m}^2\text{]}$$

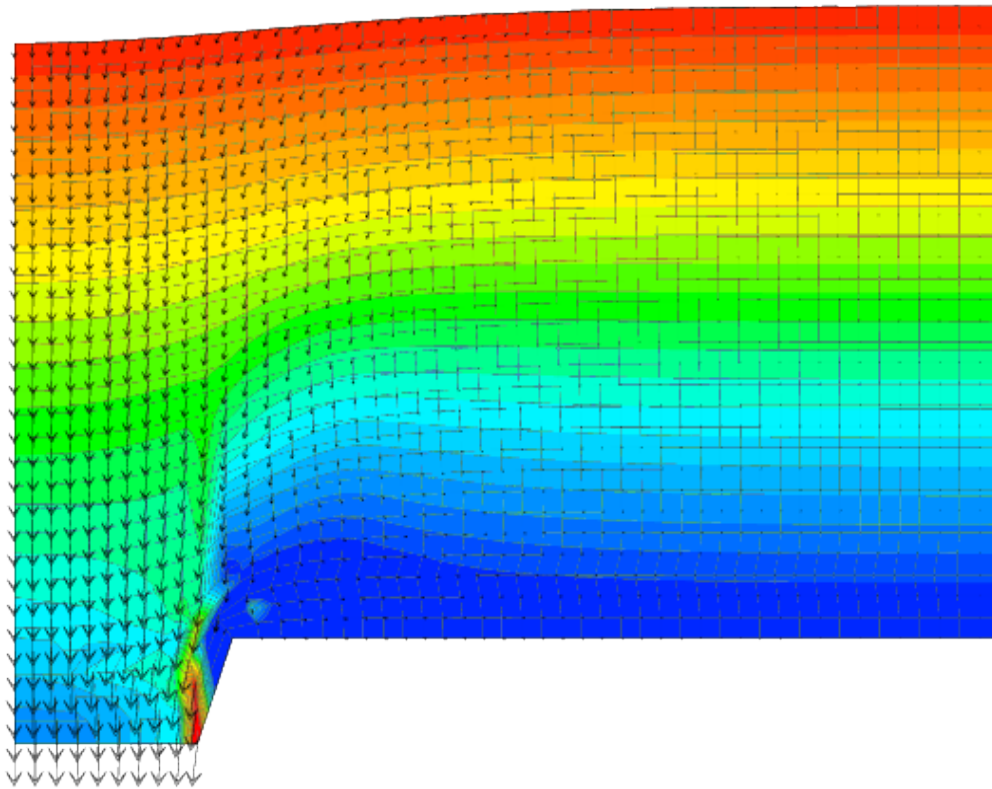
$$m = 0,75 \text{ [1]}$$

$$\nu = 0,45 \text{ [1]}$$

$$K_0 = 0,826 \text{ [1]}$$

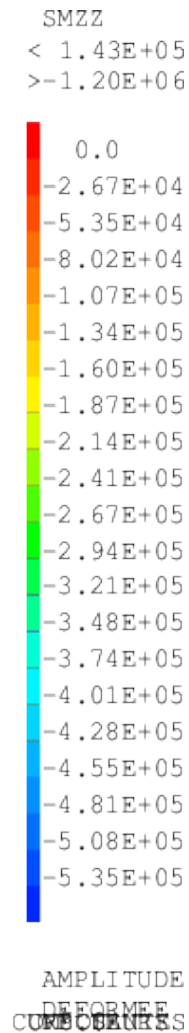
Mining subsidence – Vertical stress:

$$u_1 = 0,338 \text{ [m]}$$



$$u_0 = 1,000 \text{ [m]}$$

$$\sigma_{zz}$$



Drucker-Prager:

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$$m = 0,75 \text{ [1]}$$

$$\nu = 0,45 \text{ [1]}$$

$$K_0 = 0,826 \text{ [1]}$$

Geotechnic mining subsidence analysis:

Model height: 50m

Stiffness: high

Material: frictional, non cohesive (sand)

Mining subsidence – Vertical displacement:

Drucker-Prager:

$$\rho = 2000 \text{ [kg/m}^3\text{]}$$

$$\varphi = 30,00 \text{ [}^\circ\text{]}$$

$$c = 1,00 \text{ [kN/m}^2\text{]}$$

$$\psi = 0,00 \text{ [}^\circ\text{]}$$

$$E_{\text{ref}} = 10^7 \text{ [kN/m}^2\text{]}$$

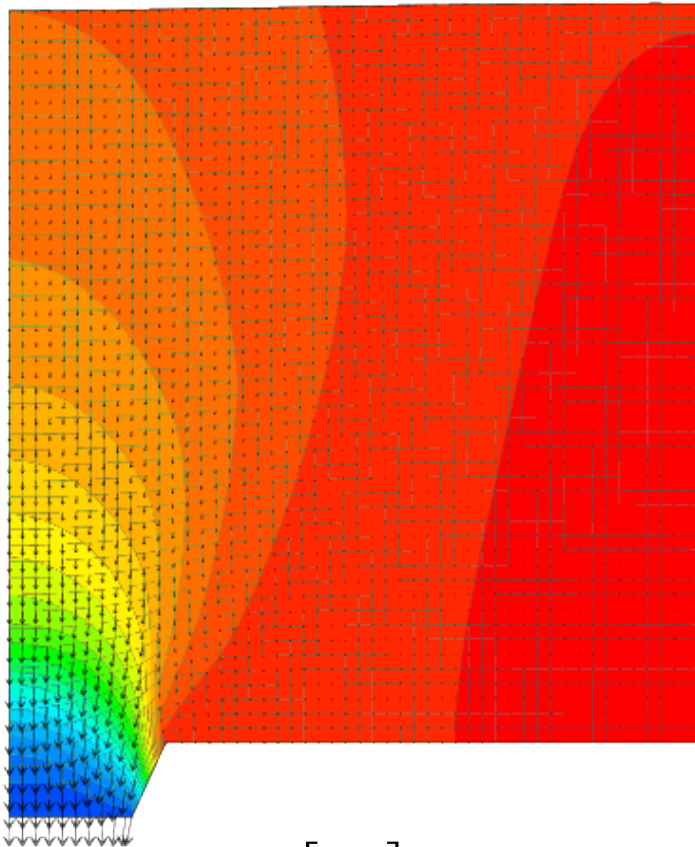
$$p_{\text{ref}} = 10^5 \text{ [kN/m}^2\text{]}$$

$$m = 0,50 \text{ [1]}$$

$$\nu = 0,33 \text{ [1]}$$

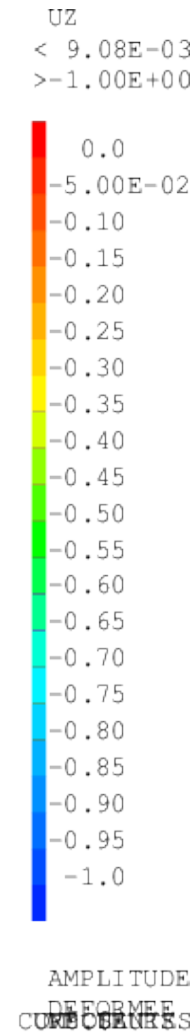
$$K_0 = 0,500 \text{ [1]}$$

$$u_1 = 0,152 \text{ [m]}$$



$$u_0 = 1,000 \text{ [m]}$$

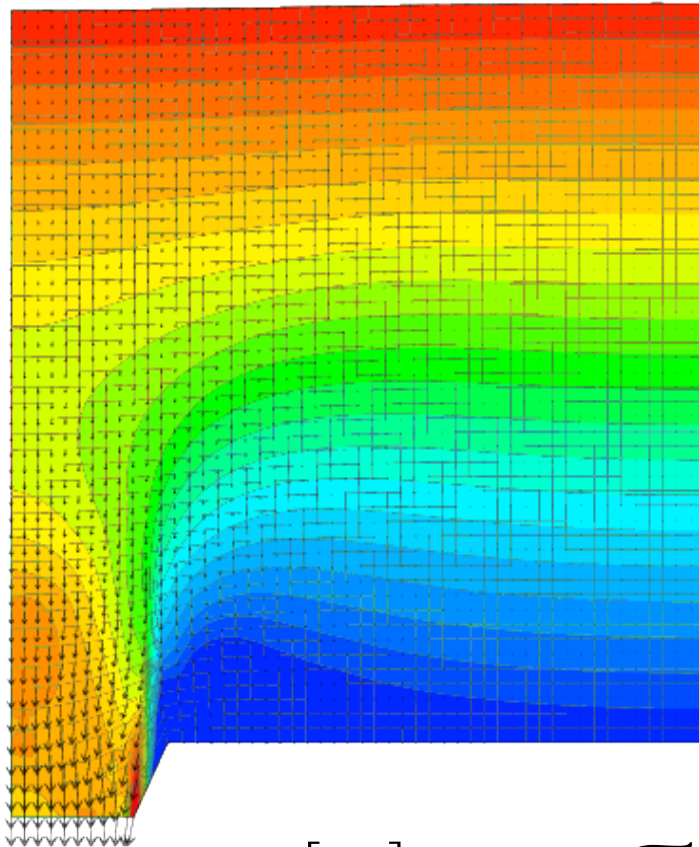
u_z



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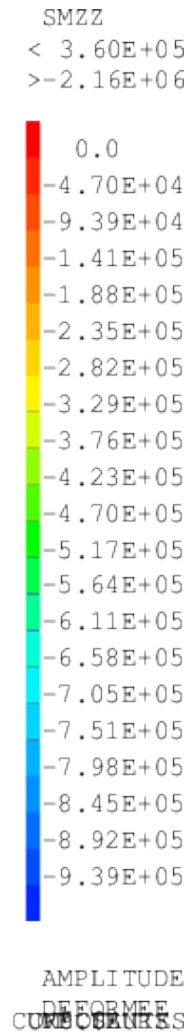
Mining subsidence – Vertical stress:

$u_1 = 0,152 \text{ [m]}$



$u_0 = 1,000 \text{ [m]}$

σ_{zz}



Drucker-Prager:

$\rho = 2000 \text{ [kg/m}^3\text{]}$

$\varphi = 30,00 \text{ [}^\circ\text{]}$

$c = 1,00 \text{ [kN/m}^2\text{]}$

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$E_{ref} = 10^7 \text{ [kN/m}^2\text{]}$

$p_{ref} = 10^5 \text{ [kN/m}^2\text{]}$

$m = 0,50 \text{ [1]}$

$\nu = 0,33 \text{ [1]}$

$K_0 = 0,500 \text{ [1]}$

Geotechnic mining subsidence analysis:

Program system Cast3M-2015-1 (fr)

Open Source (Esope, Fortran77-derivate)

Project oriented extension possible

Free license for research and education

(<http://www-cast3m.cea.fr>)

Future developments in mining subsidence analysis

Future developments in mining subsidence analysis:

**Geotechnical analysis methods
will be more intensely applied**

**Cooperation between Geodesy and
Geotechnics will be more profound
(coupling of GIS and simulation codes)**

Integration of laboratory test results

Future developments in mining subsidence analysis:

**Improvement of the prediction
performance and quality of material
behaviour models for geomaterials**

**Application of inverse methods in
combination with sensitivity analyses and
extensive modelling campaigns**

Future developments in mining subsidence analysis:

**Use of parallel computational resources
(fat nodes are increasingly available)**

**Computation of large models in the
framework of true mine scale modelling**

**Consideration of coupled thermic,
mechanic and hydraulic problems**

Geotechnic mining subsidence analysis:



**“Green”
HPC-Cluster:**

**35 x VIA-C3-1GB
4 x iATOM-4GB**

Software:

**openSuSE Linux
Tumbleweed**

**SLURM
Resource Manager**

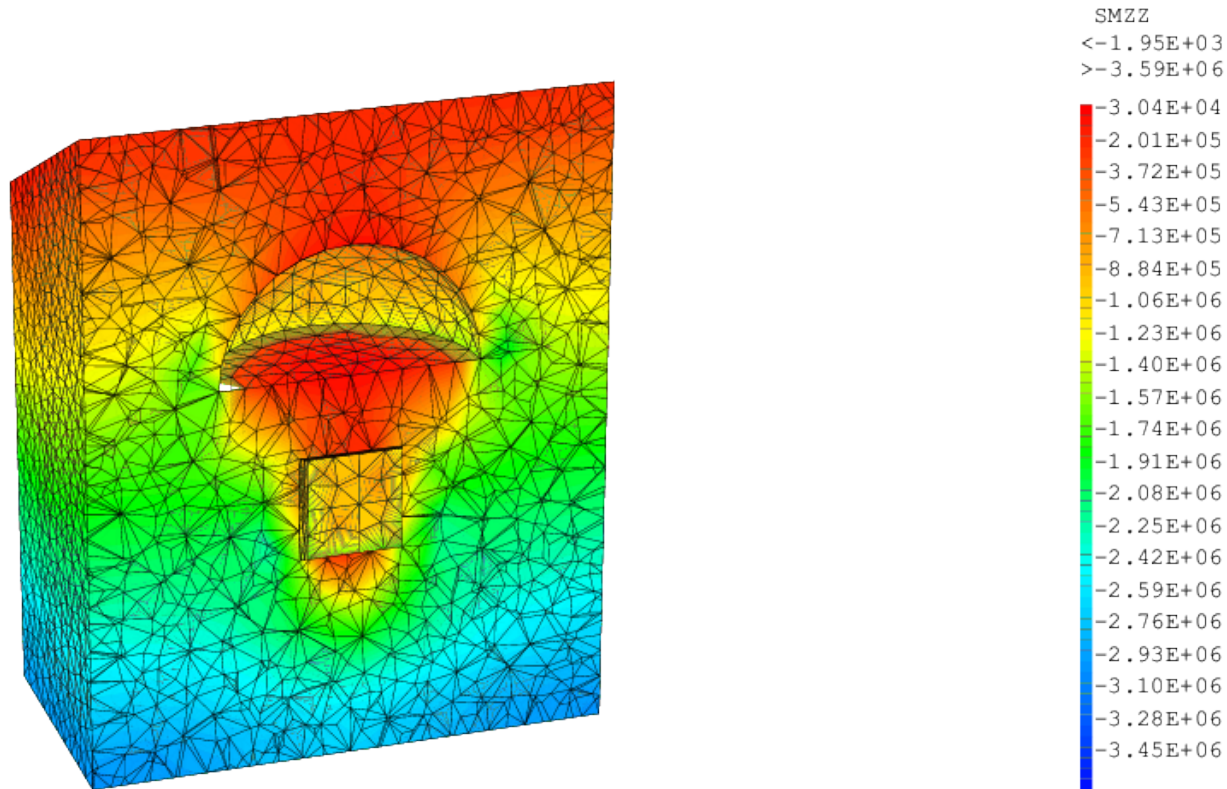
**Python
Scripting
+
Cast3M-2015-1
FEM Toolbox**

**Additional conceptual studies
for diverse typical
geotechnical applications
of the Cast3M
FEM analysis framework**



Mine scale modelling (Qualitative study)

Mine scale modelling (small scale here):



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NBEL=42k

Excavation procedure in Cast3M:

Efficient excavation procedure is available with virtual “time dependent” formulation of the material model parameters

From a stable initial state under external and self weight load, the stiffness and density parameters of the cavern are stepwise reduced to a very small value

Cast3M as solver module:

The MED (V3.2.0) library is available for data transfer between codes

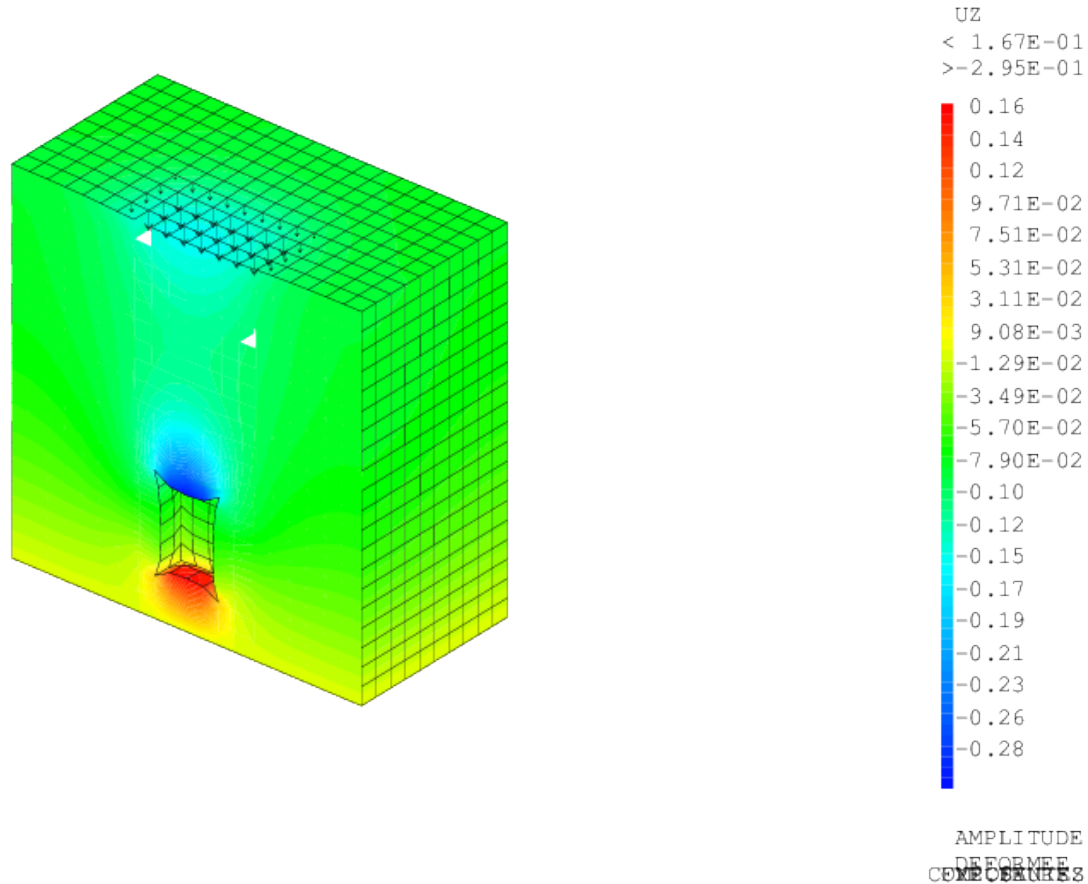
Coupling to GMSH is straightforward but post processing in Cast3M can be more powerful and advantageous

Additional coupling to SALOME through data transfer with the .sauv file format

Ground and structure interaction induced by underground openings such as caverns, tunnels or void spaces

**(Qualitative study and patch test
for excavation procedure)**

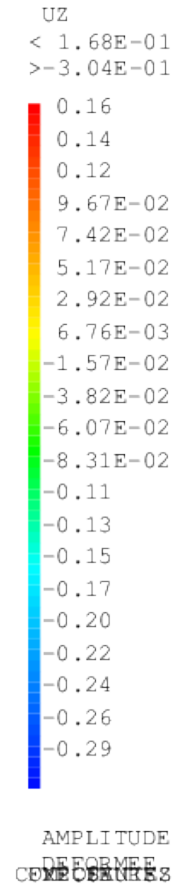
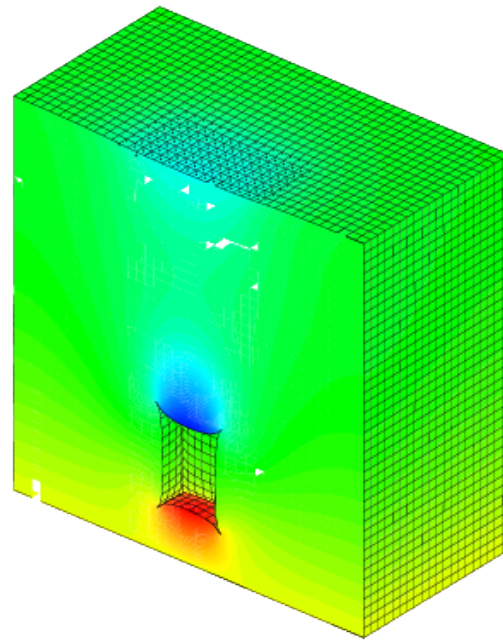
Ground and structure interaction:



NBEL=8k

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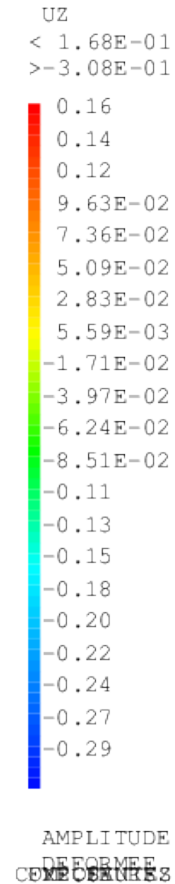
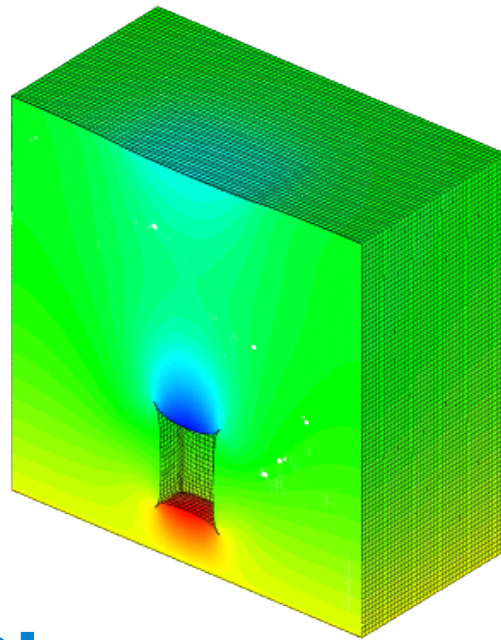
Ground and structure interaction:



NBEL=64k

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Ground and structure interaction:



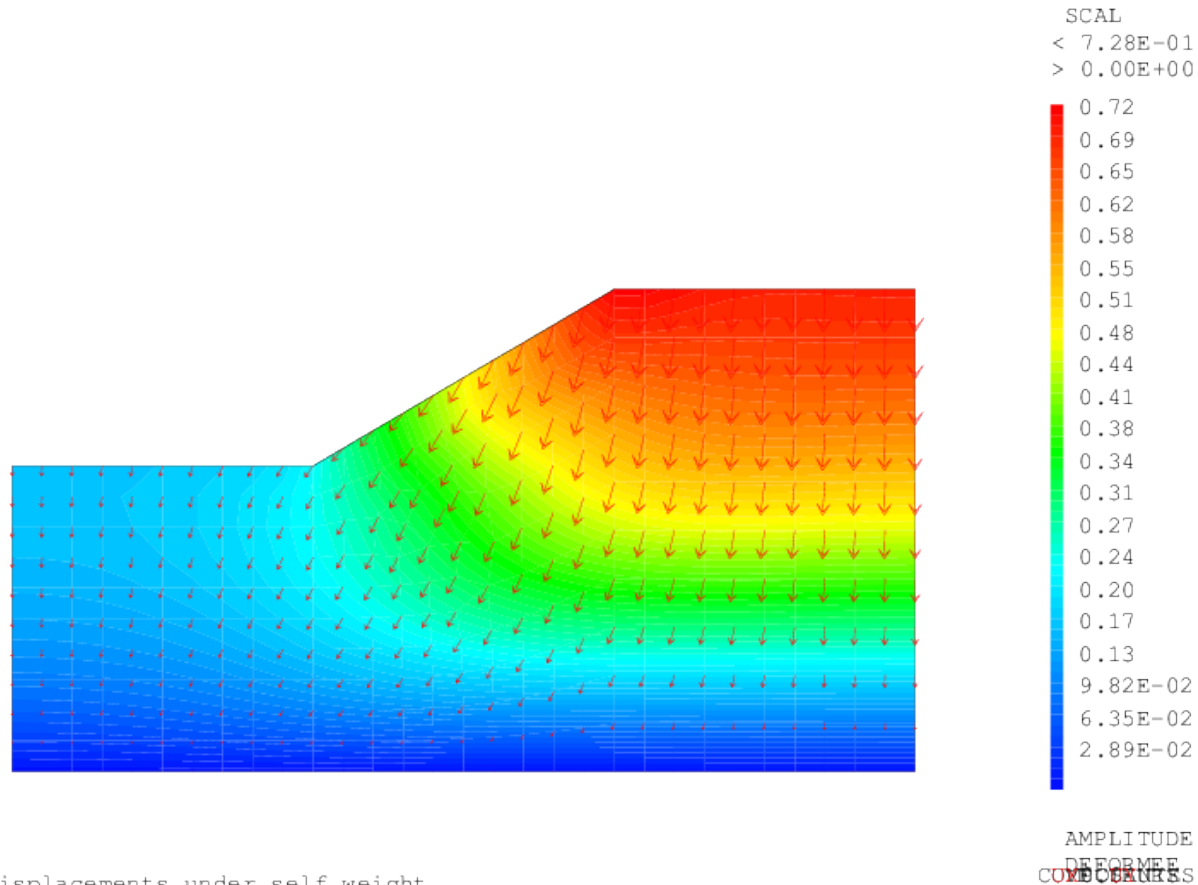
NBEL=512k

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Slope stability analysis for the proof of the overall stability of a geotechnical system

(Qualitative study)

Slope stability – self weight deformations:

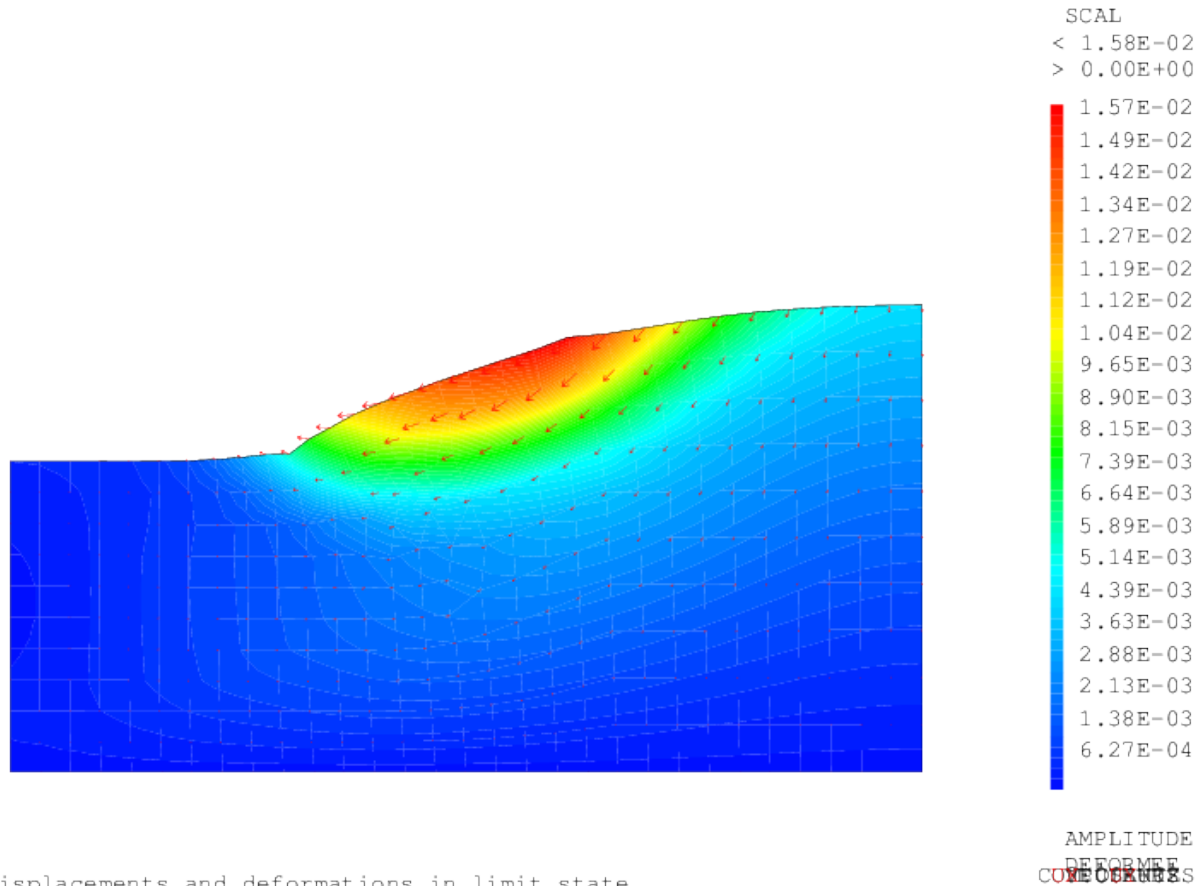


Factor of safety or Utilisation factor calculation procedure:

**Calculation of a stable initial stress and
corresponding deformation state**

**Recursive reduction of the shear and
tensile strength until a convergence to a
prescribed tolerance is still obtainable**

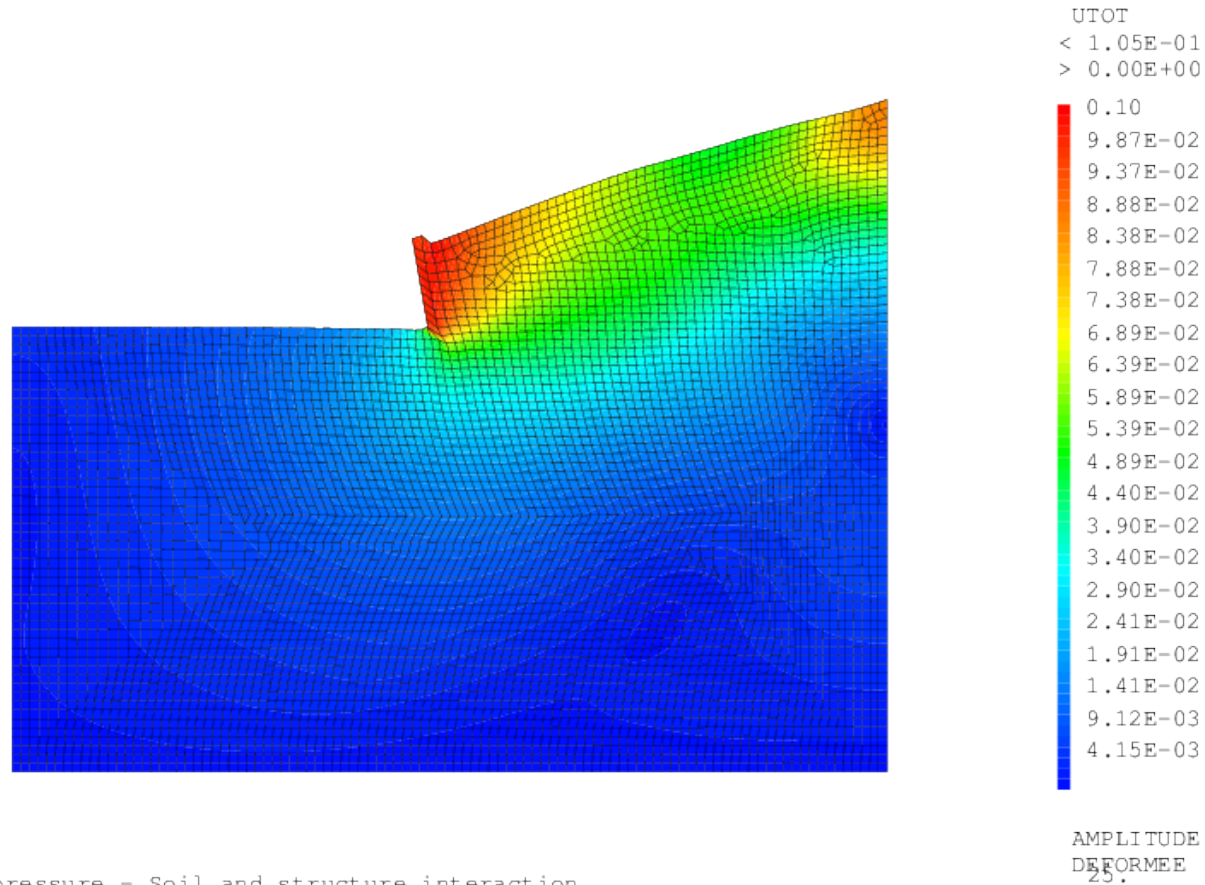
Slope stability – deformations in limit state:





Supporting construction design (Qualitative study)

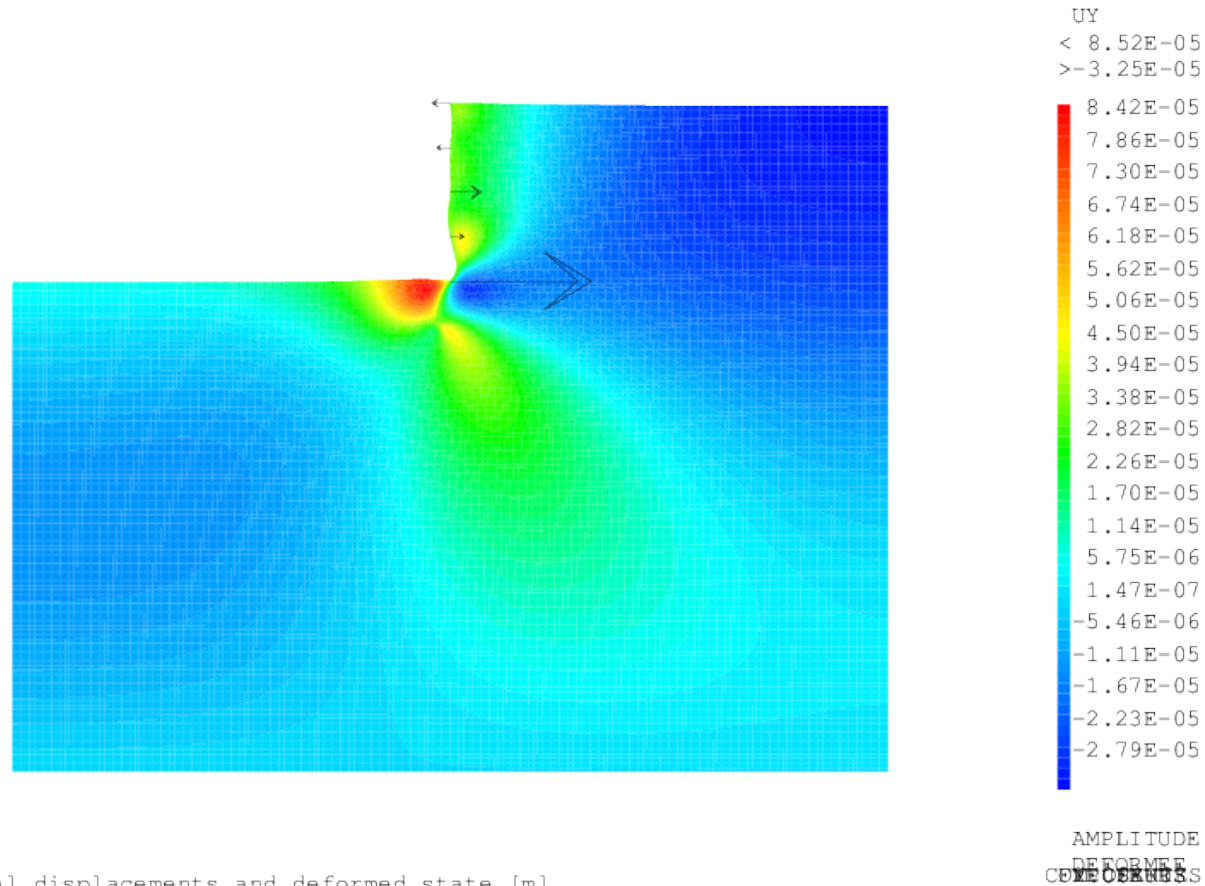
Supporting construction design:





Construction trench wall design (Qualitative study)

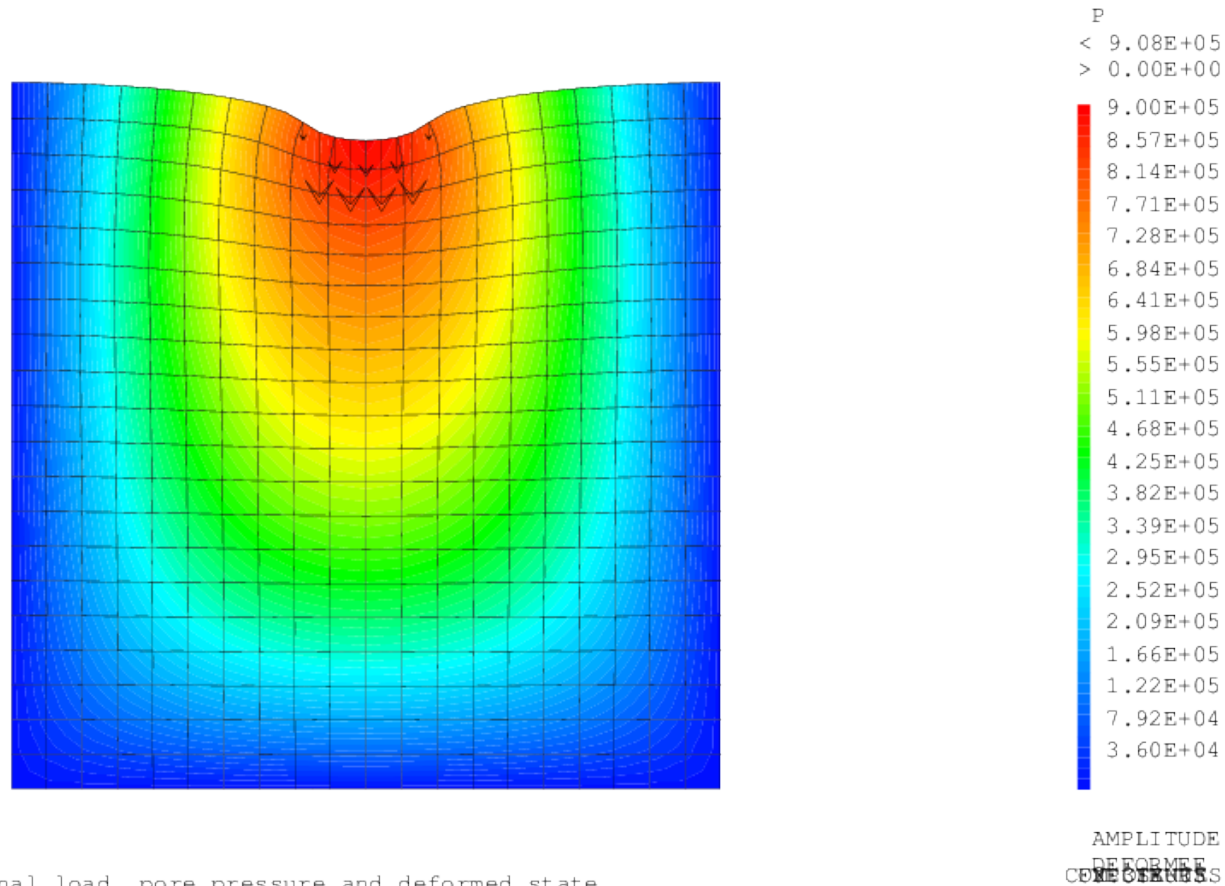
Construction trench wall design:





Spatial consolidation problem (Qualitative study)

Spatial consolidation problem:



Further application fields:

**Dynamic loading of structures in
time and frequency domain**

Soil and structure interaction

**Groundwater flow and contamination
transport modelling**

Geothermal applications



Conclusions

Summary:

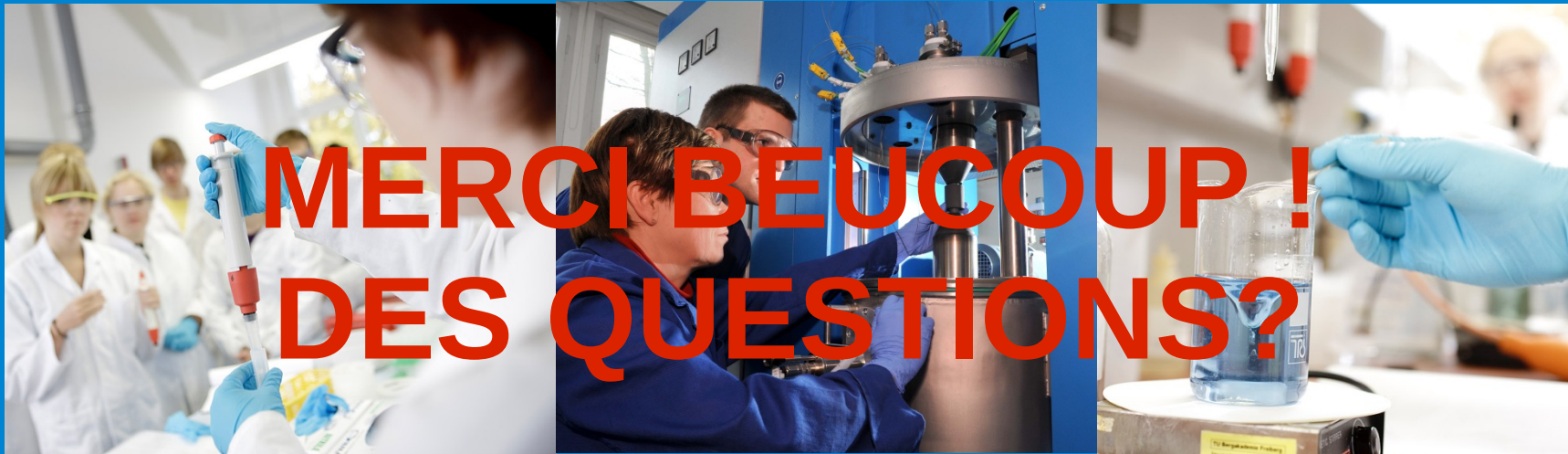
Cast3M is an excellent and unique open source programme for education, research and commercial use in Geotechnics

With minor extensions and adjustments, Cast3M can also compete with known commercial geotechnical codes on the market with WORLDWIDE HIGH DEMAND



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